

# ВСЕ О ТРИОНАХ

## *Trions at low electron density limit*

- 1. Charged exciton-electron complexes (trions)
- 2. Singlet and triplet trion states
- 3. Modulation doped QWs
- 4. Trions in optical spectra
- 5. Action of magnetic fields on the trions

## *Trions at high electron density limit*

- 6. Combined exciton cyclotron resonance
- 7. Combined trion cyclotron resonance
- 8. Combined exciton electron processes in PL spectra
- 9. Trion Zeeman splitting

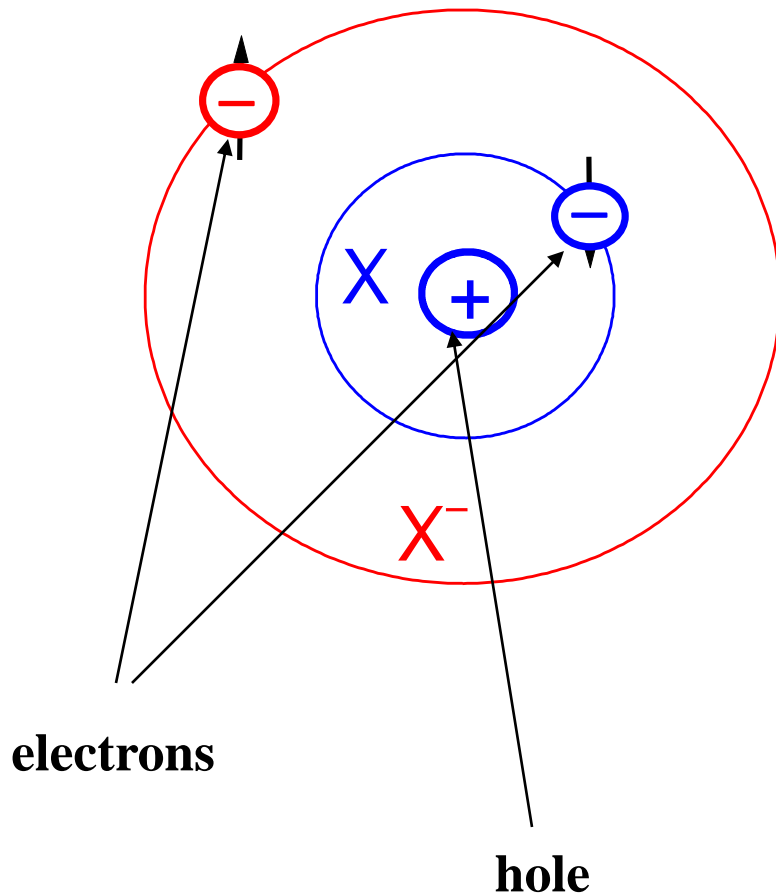
# LOW 2DEG DENSITY

Two electrons+one hole states

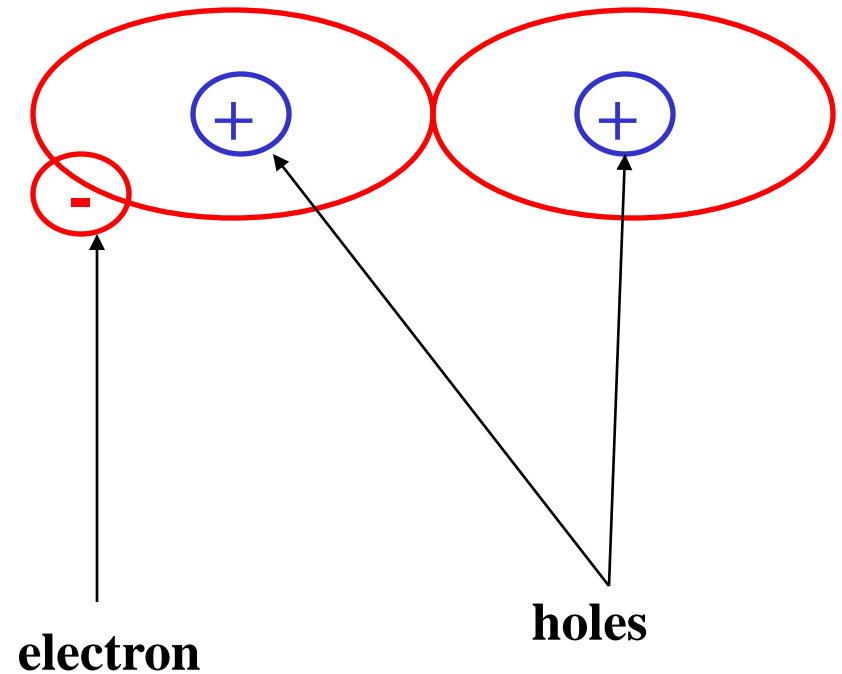
- Trions at weak magnetic fields
- Trions at high magnetic fields
- Excited states of trion

# Charged exciton – electron complex (trion)

**Negatively charged Trion  $X^-$**   
*similar to ion  $H^-$*



**Positively charged Trion  $X^+$**   
*Similar to ionized molecule  $H^+$*



# Singlet and Triplet trion states

Wavefunction for two electrons in the trion

$$\varphi(1,2) = U(1,2)\chi(1,2)$$

Spatial part of the wavefunction

$$U_{nlm}^0 = \frac{1}{\sqrt{2}} \left[ u_1(\vec{r}_1) u_{nlm}(\vec{r}_2) \pm u_1(\vec{r}_2) u_{nlm}(\vec{r}_1) \right]$$

Singlet state +  $S_z = 0 \propto e^{-\alpha(\vec{r}_1 + \vec{r}_2)}$

Triplet state -  $S_z = \pm 1, 0$

$$\left. \begin{array}{l} S_z = +1 \\ S_z = 0 \\ S_z = -1 \end{array} \right\} \text{triplet}$$

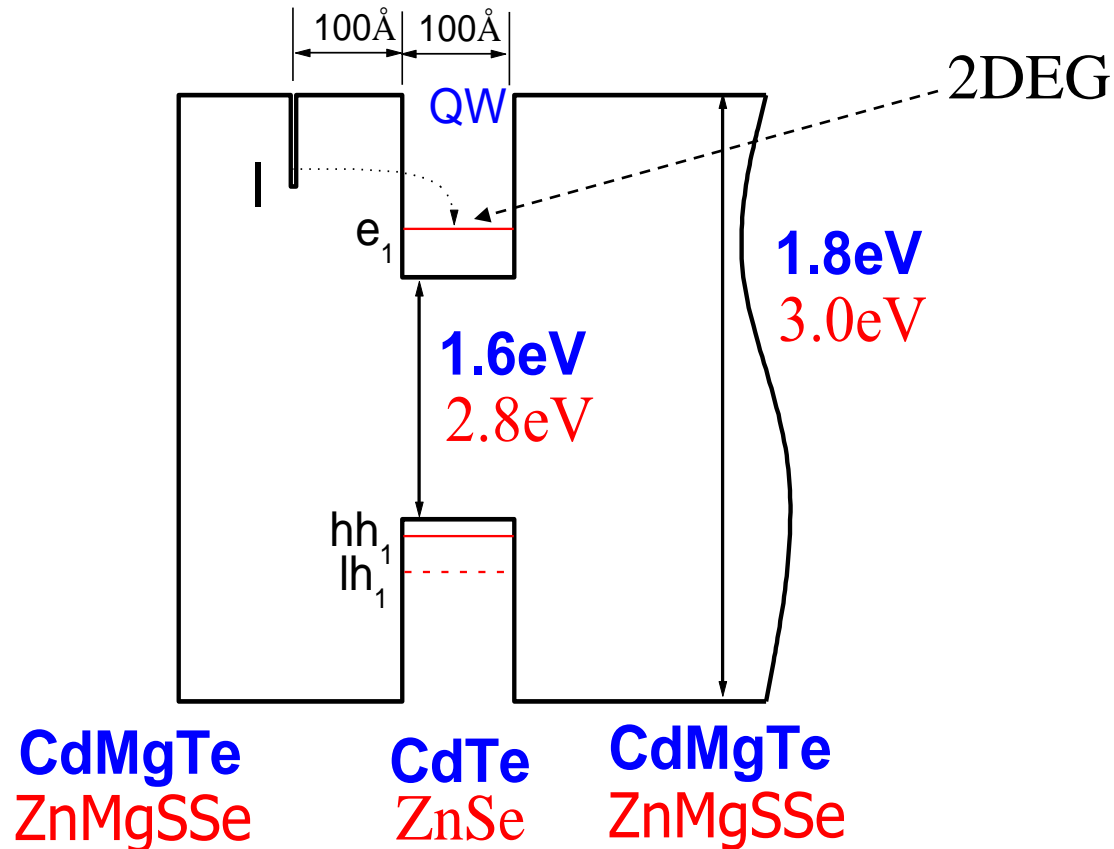
$$S_z = 0 \quad \text{singlet}$$

$U_{nlm} \neq 0$ , if  $l \neq 0$  one electron is in  $1S$  and the second is in  $2P$  state – dark triplet

Or if  $n \neq 1$  one electron is in  $1S$ , and the second is in a  $2S$  state bright triplet

# Experimental studies of trions

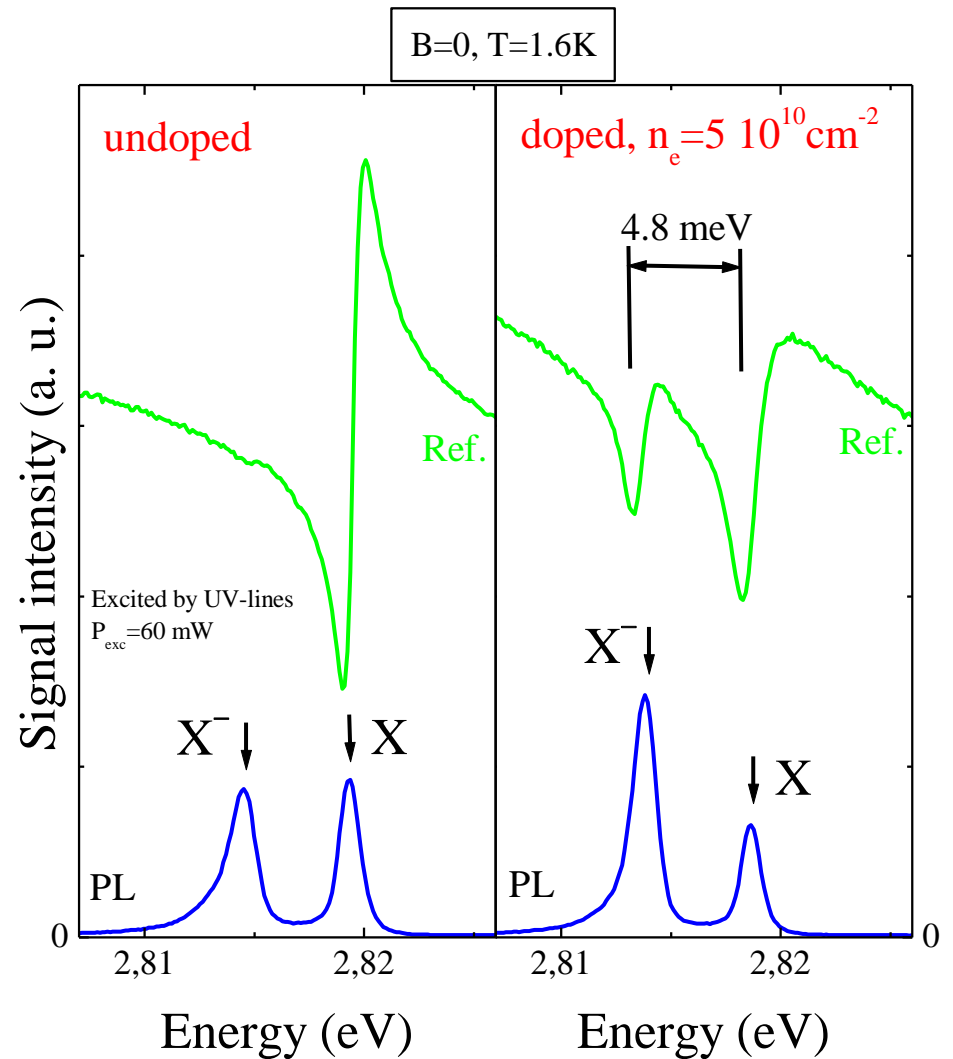
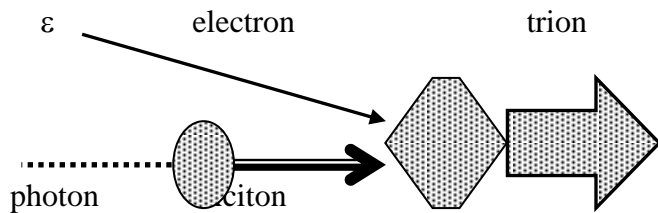
# Modulation doped structures



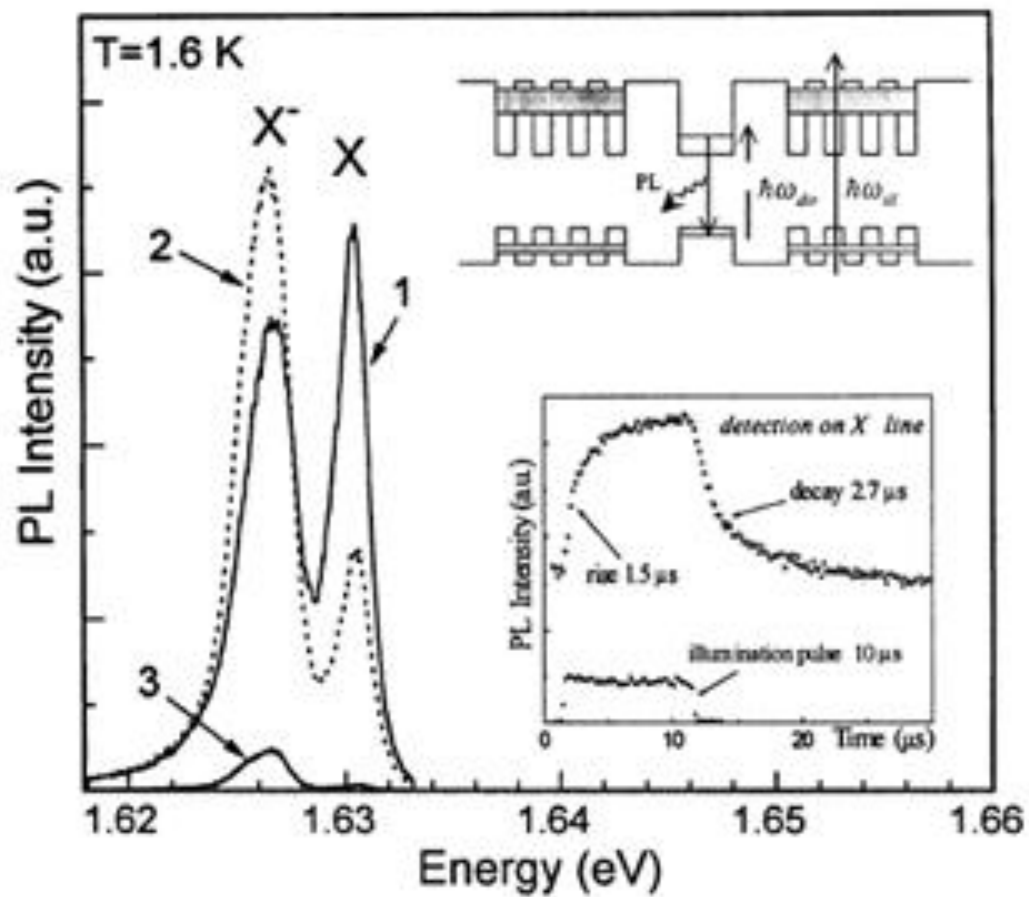
2DEG density varied from  $n_e = 5 \cdot 10^9 \text{ cm}^{-2}$  to  $9 \cdot 10^{11} \text{ cm}^{-2}$

# Optical processes with the trion participation

Trion formation time in ZnSe structures is of the order of 2–4 psec

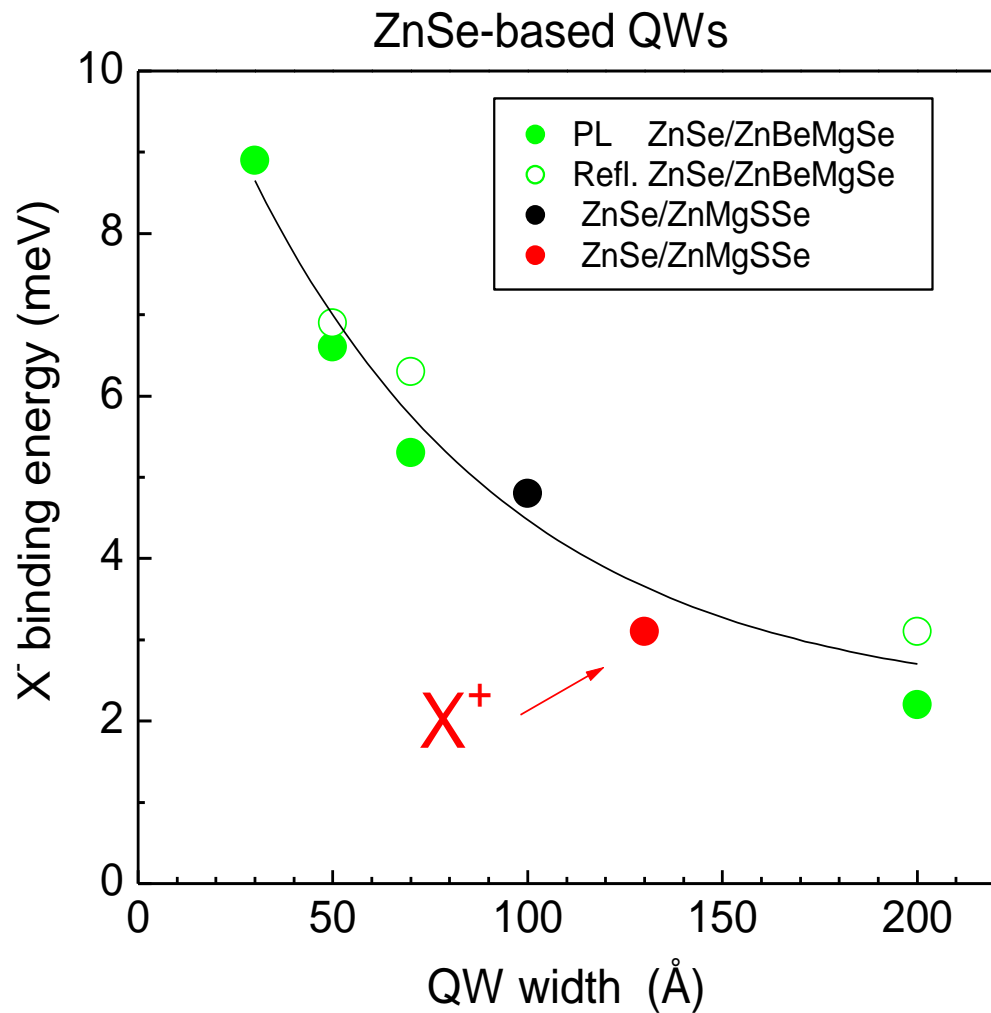


## Изменение концентрации при подсветке



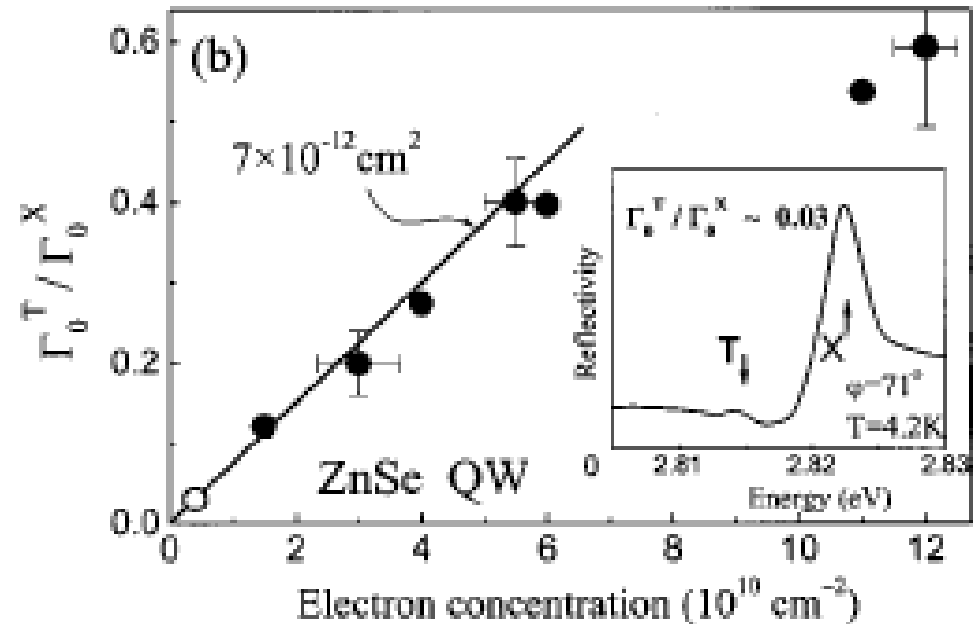
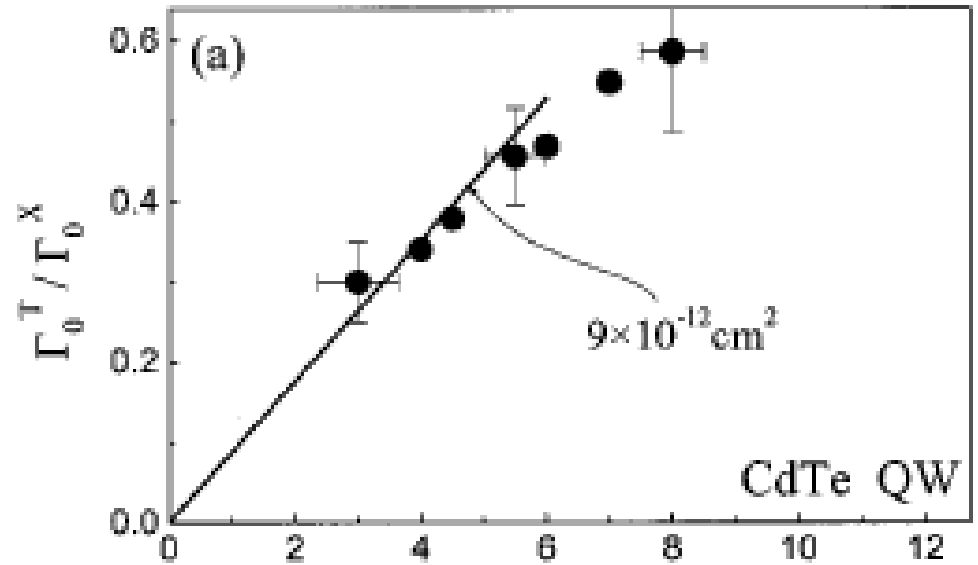


# Зависимость энергии связи триона от ширины ямы



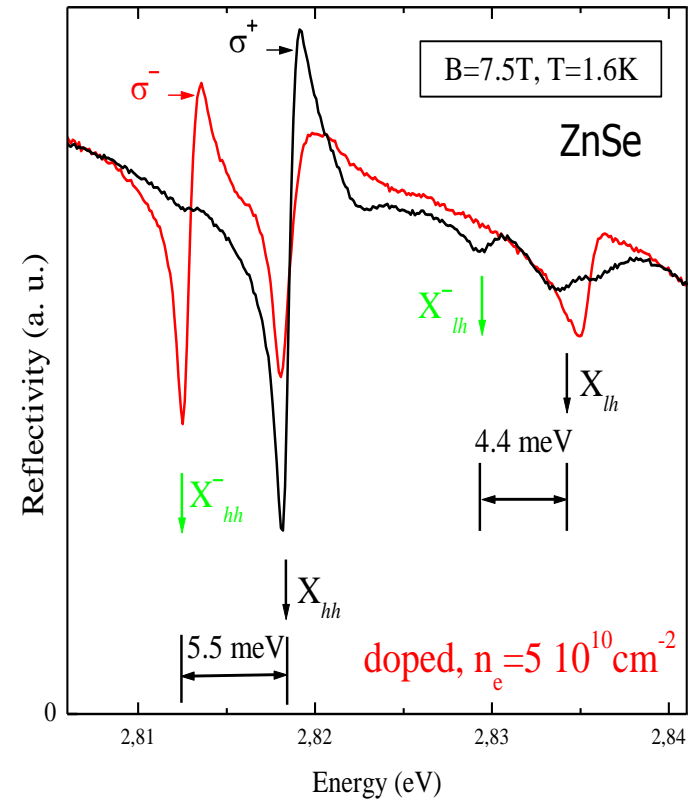
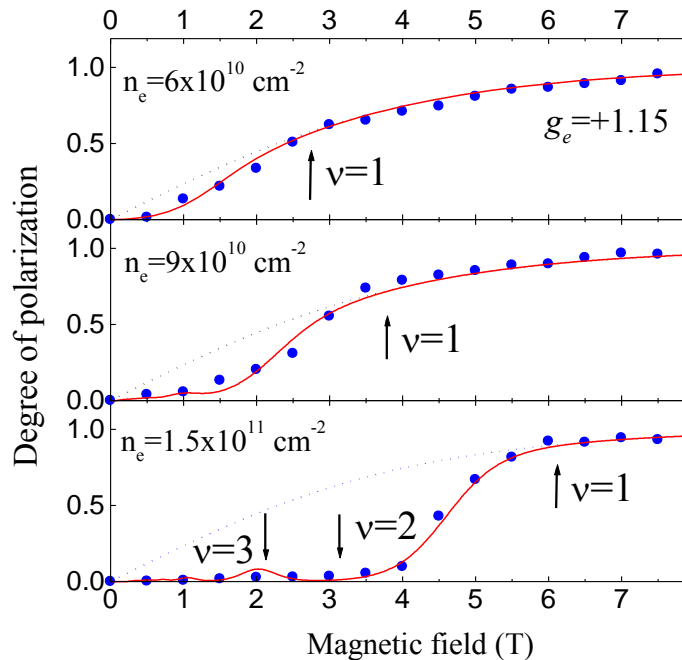
Сила осциллятора экситона  
 приходящаяся на элементарную  
 ячейку равна силе осциллятора  
 триона на один электрон, также  
 Как для связанных экситонов

$$\frac{\Gamma_0^T}{\Gamma_0^X} = C n_e$$



Singlet and Triplet  
Trion states in magnetic fields

# Singlet trion in magnetic fields

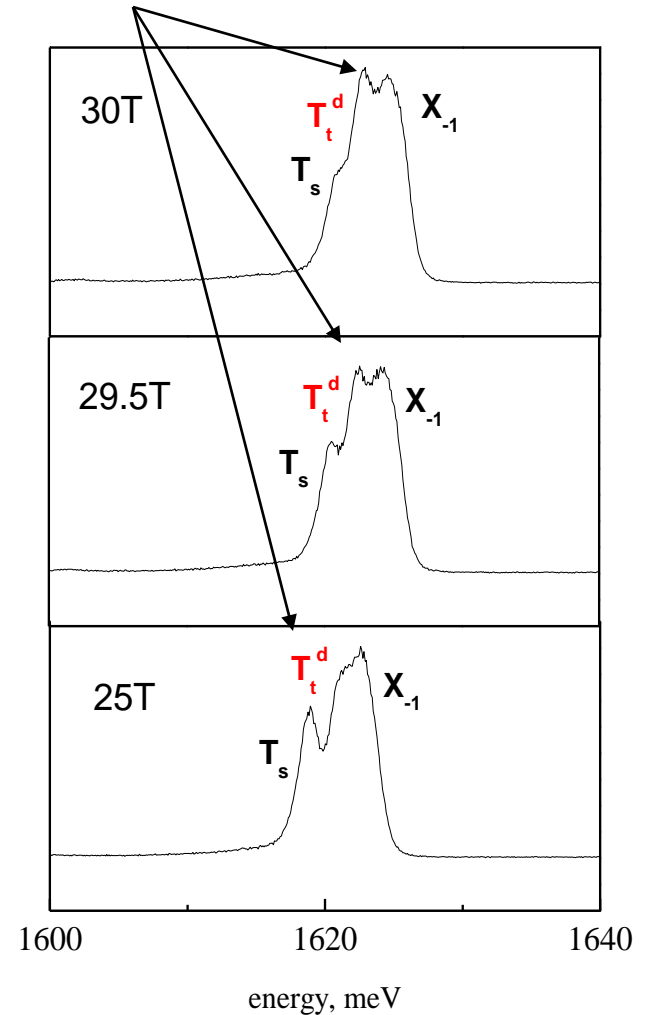
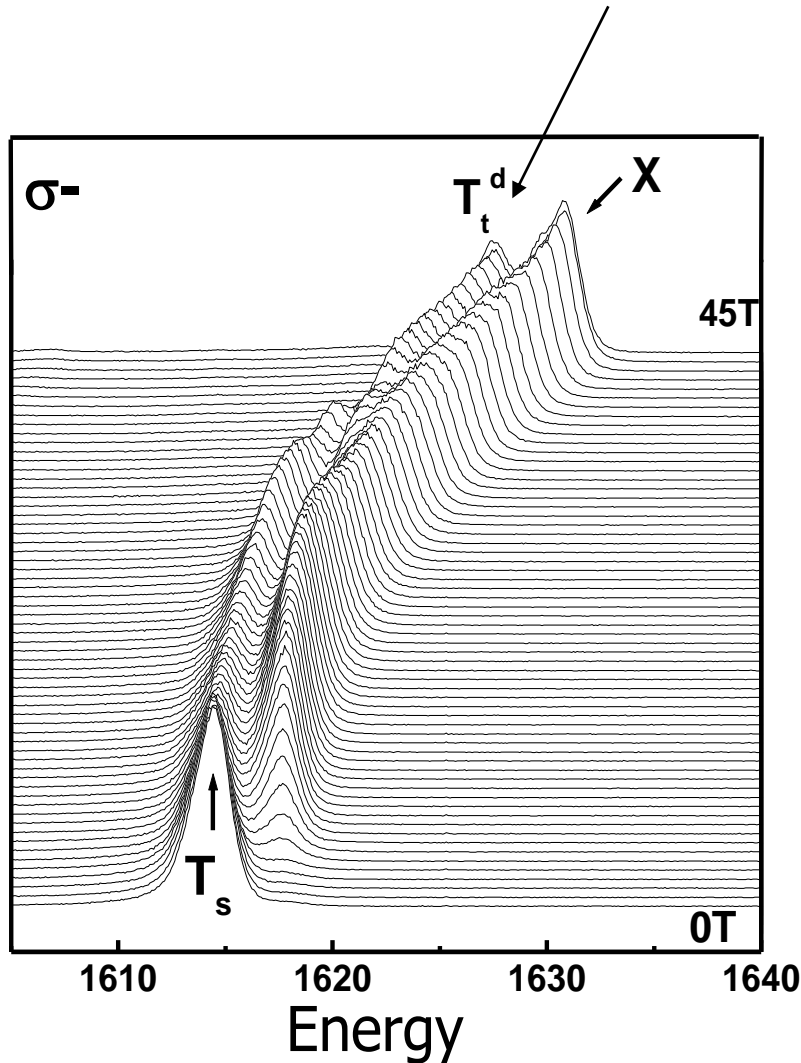


The circular polarization of the trion absorption (reflectivity line) in magnetic fields can be used to determine electron concentration by pure optical method

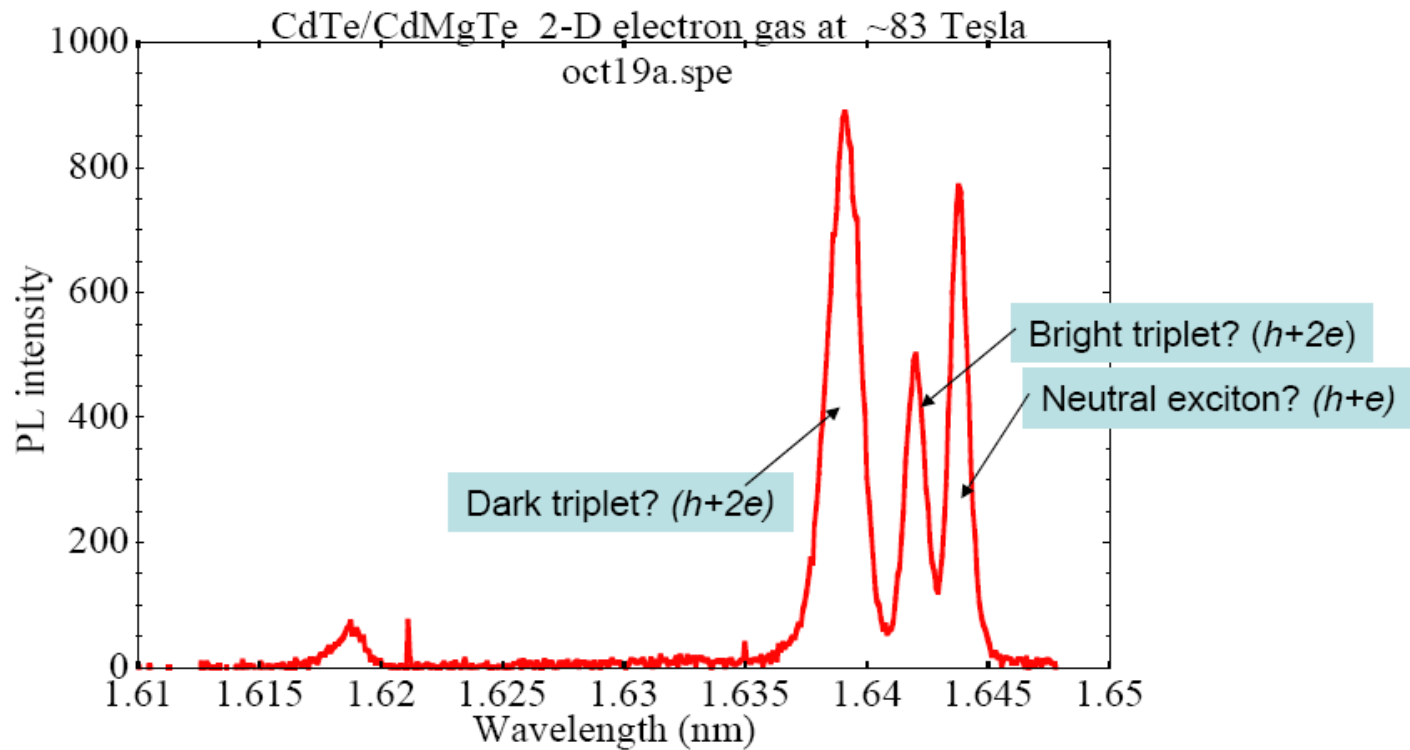
$X_{hh}^-$  and  $X_{hh}^+$  resonances appear in opposite circular polarizations

# Triplet trion in high magnetic fields

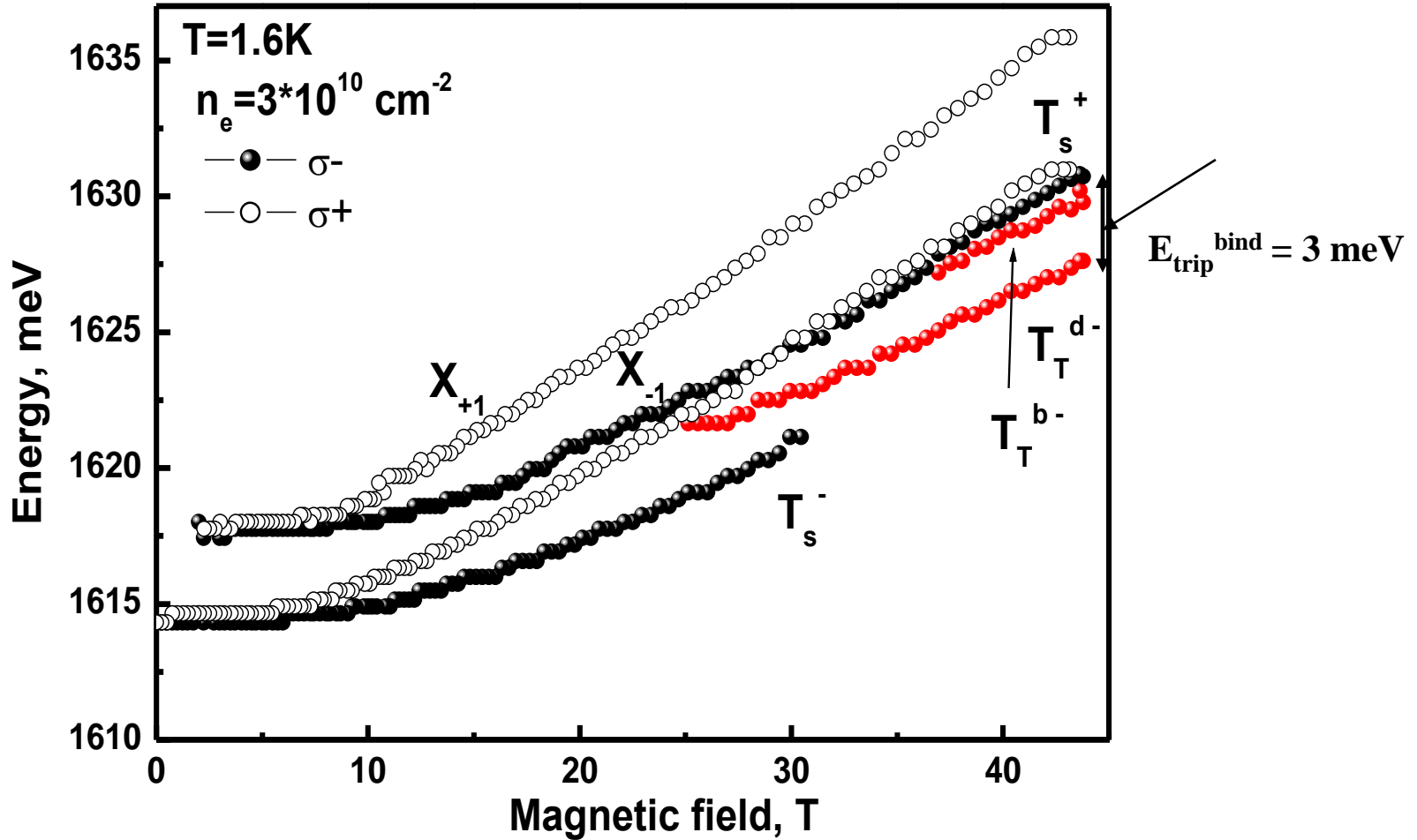
Photoluminescence



**PL spectra: CdTe/CdMgTe 2D electron gas at 1.5 K at ~83 T (in 100T LP)**



# Singlet and Triplet in high fields



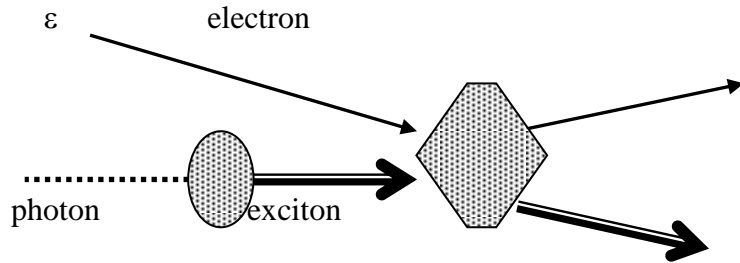
# EXCITON-ELECTRON SCATTERING

(excited states of a trion in magnetic  
fields)

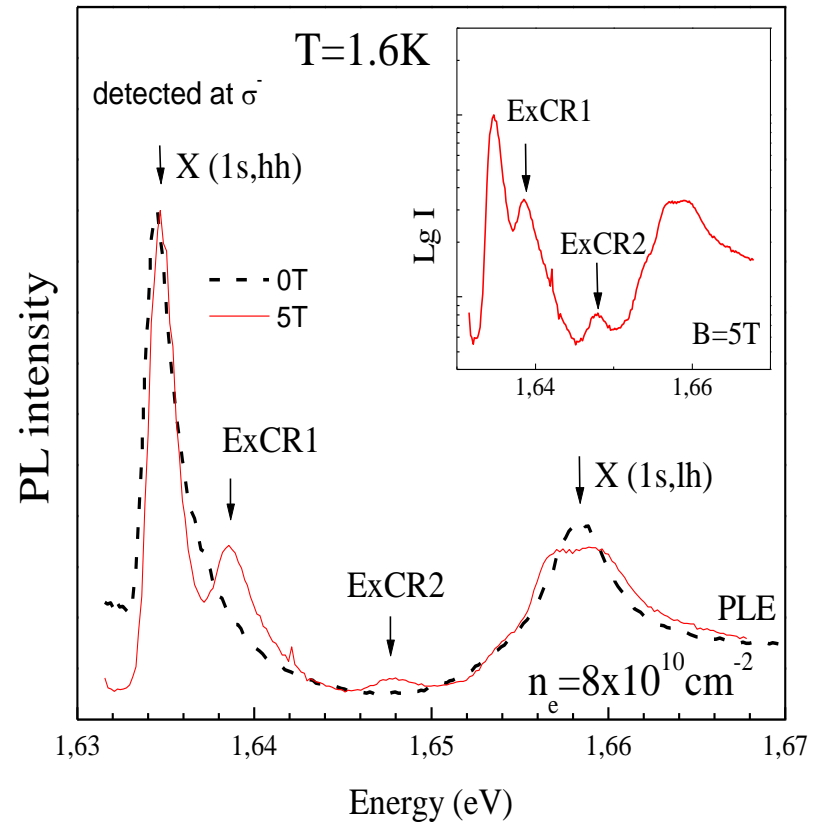


# Exciton – electron scattering

## Exciton – electron scattering



In magnetic fields in QWs the exciton electron scattering leads to the electron transitions between Landau levels - **ExCR**



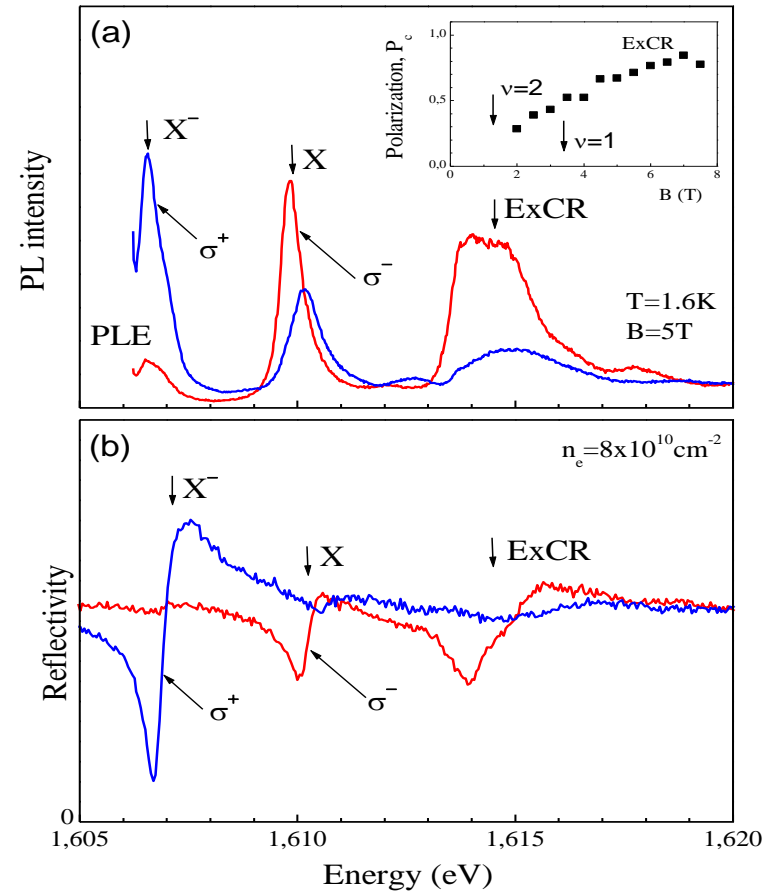
The scattering leads to high energy tail of the exciton absorption line. In magnetic fields it splits into separate lines because the electron spectrum becomes discrete = excited states of trions in magnetic fields.

We can neglect the trion binding energy because  $E_{ex}^b \gg \hbar\omega_c \gg E_{Tr}^b$

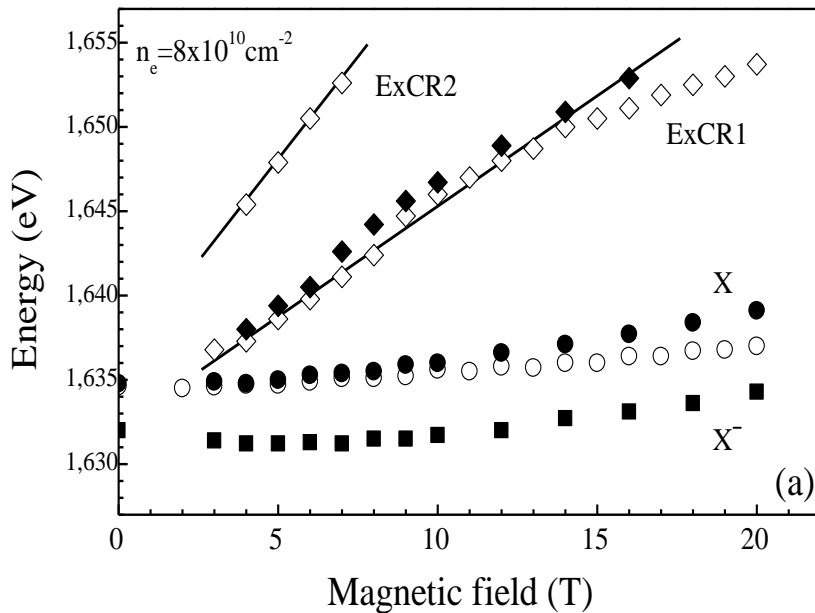


$$\frac{1}{2}\hbar\omega_e^c + \hbar\omega = E_{exc} + \frac{3}{2}\hbar\omega_e^c$$

The intensity of the ExCR absorption line is comparable with the intensity of the exciton line

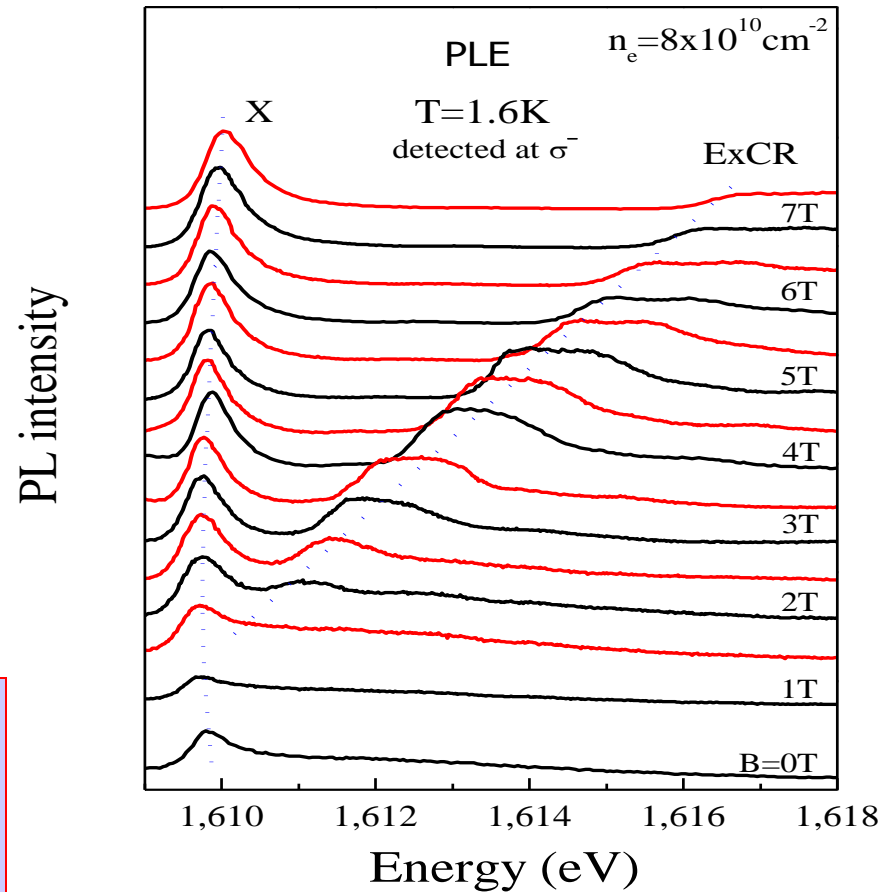


# Combined exciton –cyclotron resonance ExCR



The ExCR line shifts LINEARLY from the exciton resonance to high energies with increase of magnetic fields

$$\hbar\omega_{\text{ExCR}} = N\hbar\omega_e^c \left(1 + \frac{m_e}{M}\right)$$

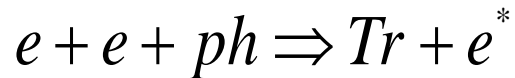


Combined processes in  
Dense 2DEG

Three electrons+one  
hole states

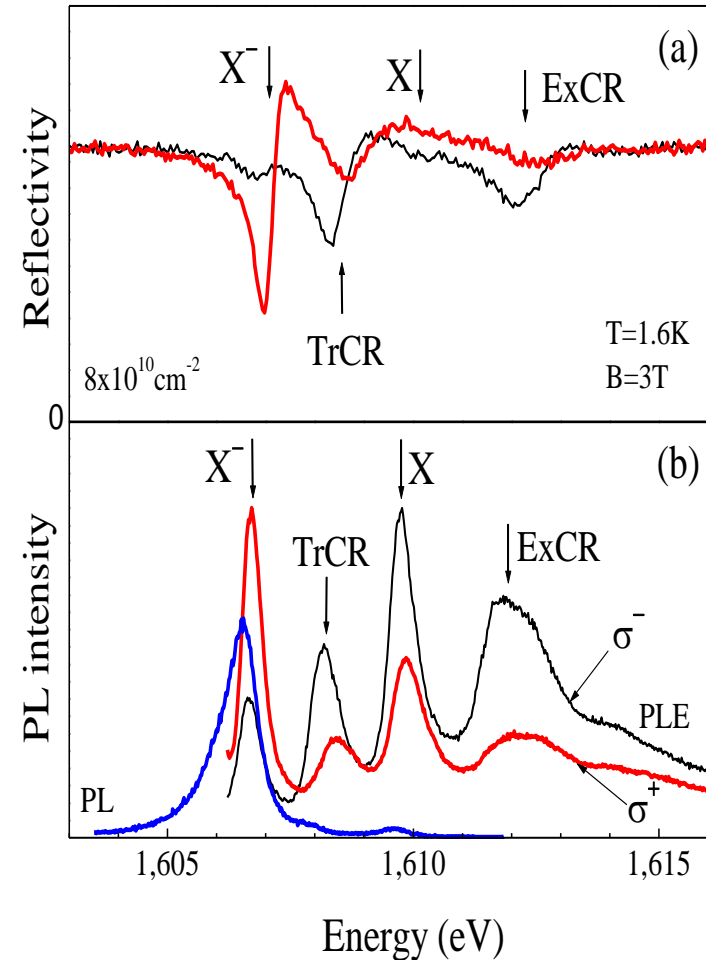
# In the dense 2DEG two-electron processes emerge in the spectra TrCR

There are two electrons in the initial state; an incident photon creates an exciton which binds with one of the electrons forming a trion; and the second electron excites on the second Landau level

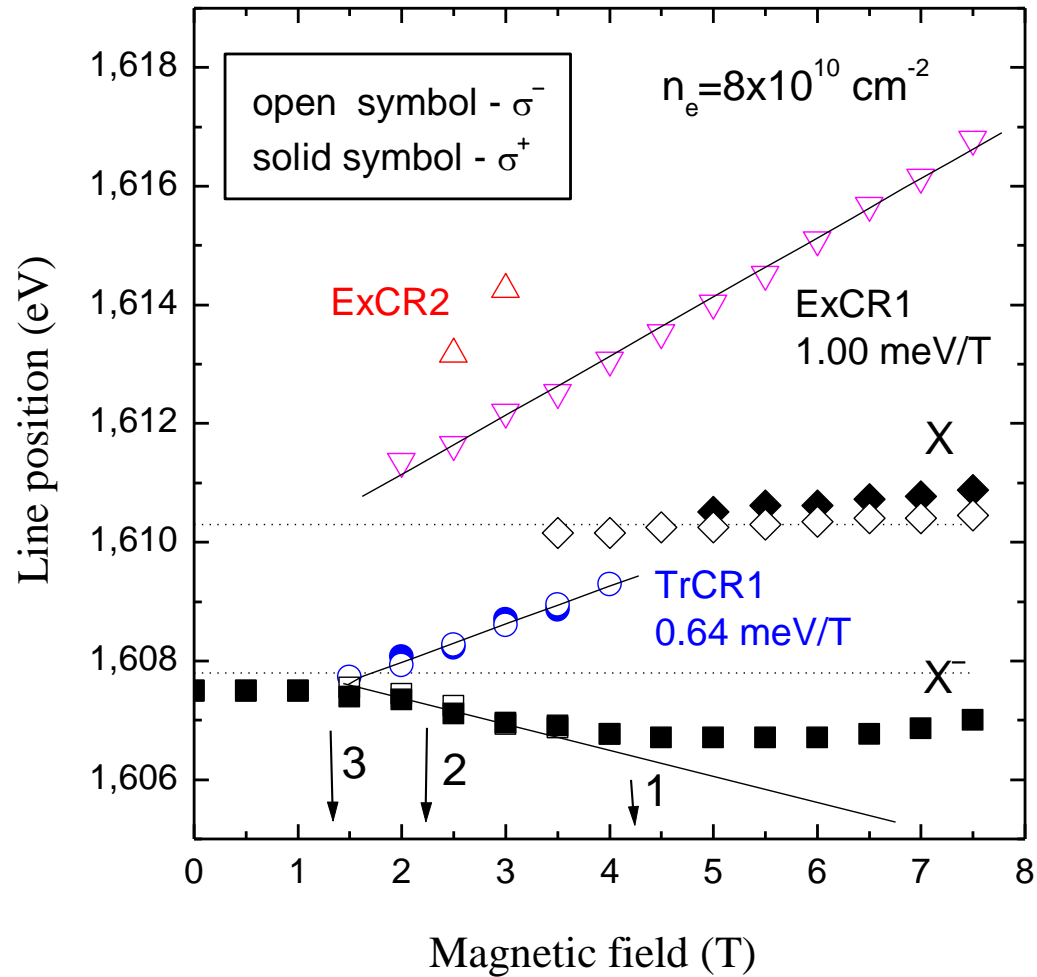


$$\frac{1}{2}\hbar\omega_e^c + \frac{1}{2}\hbar\omega_e^c + \hbar\omega = E_{tr} + \frac{3}{2}\hbar\omega_e^c$$

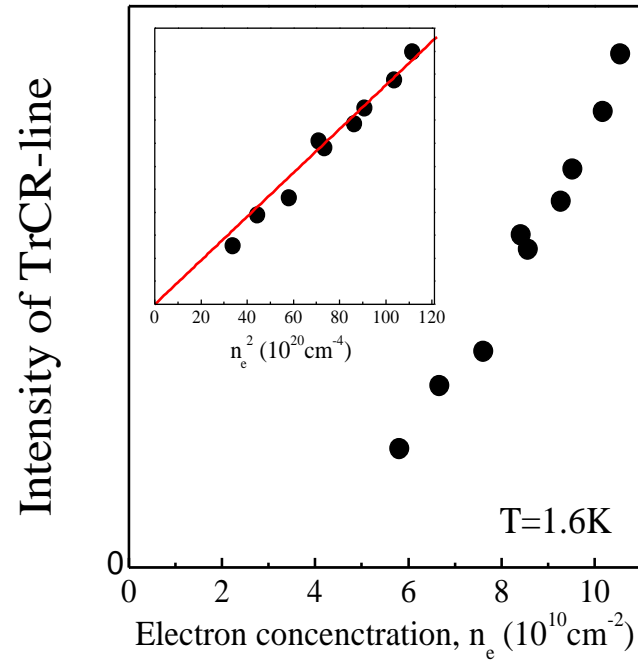
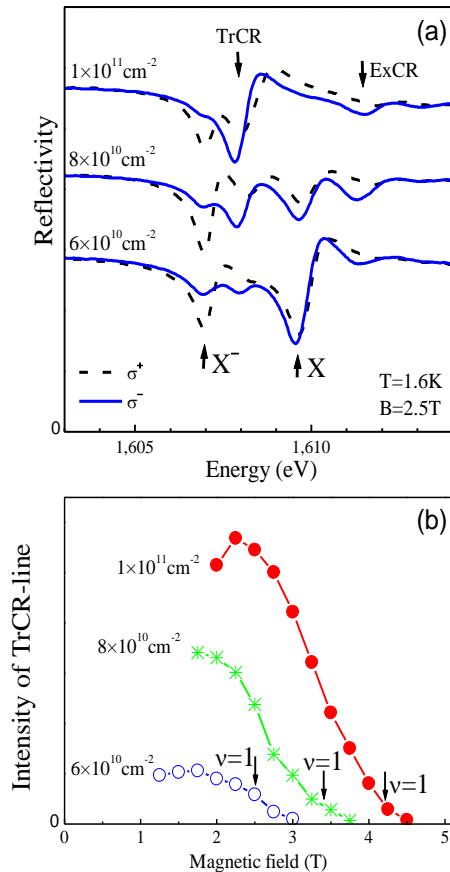
$$\hbar\omega = E_{tr} + \frac{1}{2}\hbar\omega_e^c$$



# Trion Cyclotron Resonance



Line of the TrCR is observable at filling factors  $> 1$ .  
 The intensity of the TrCR line is proportional to the second  
 power of the 2DEG density

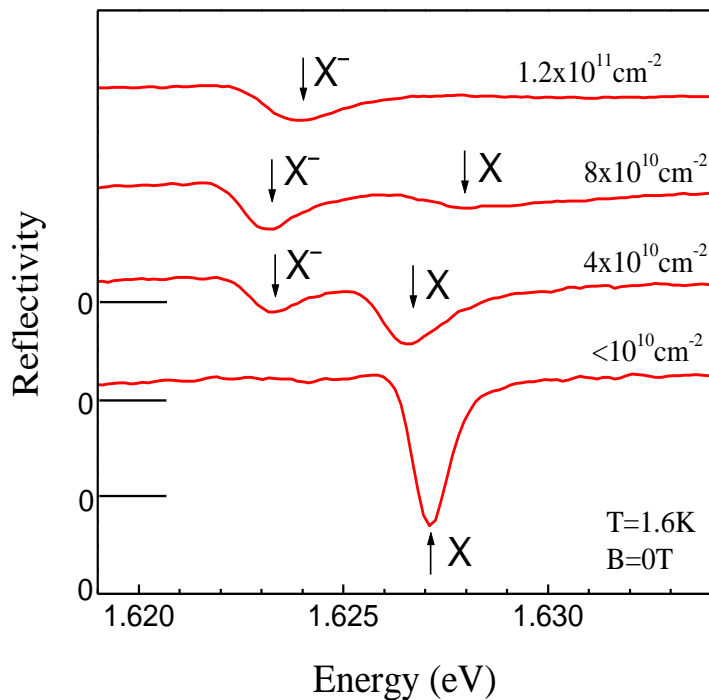


Surprising Trion stability against free  
electron screening

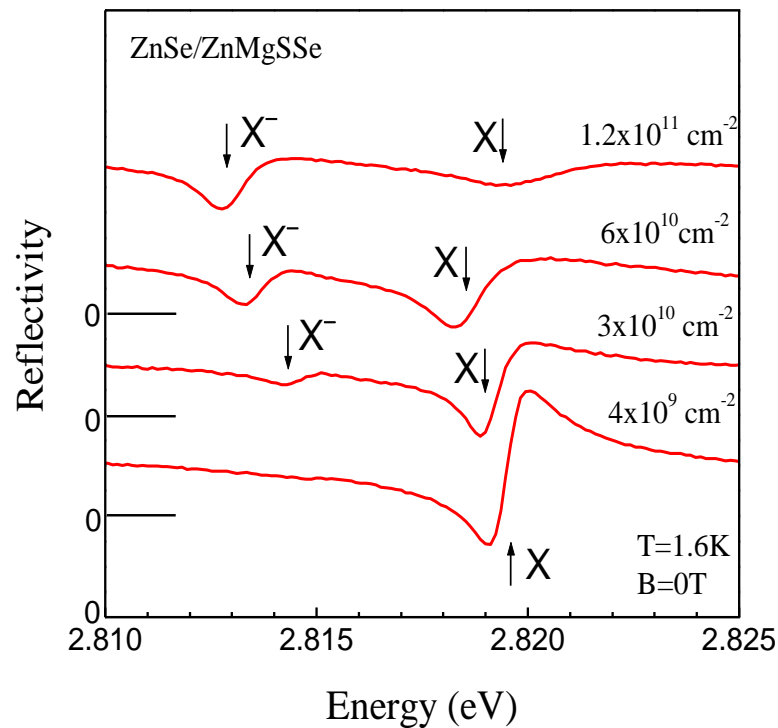


Экситон исчезает из спектра при относительно малых концентрациях электронов, а трион остается

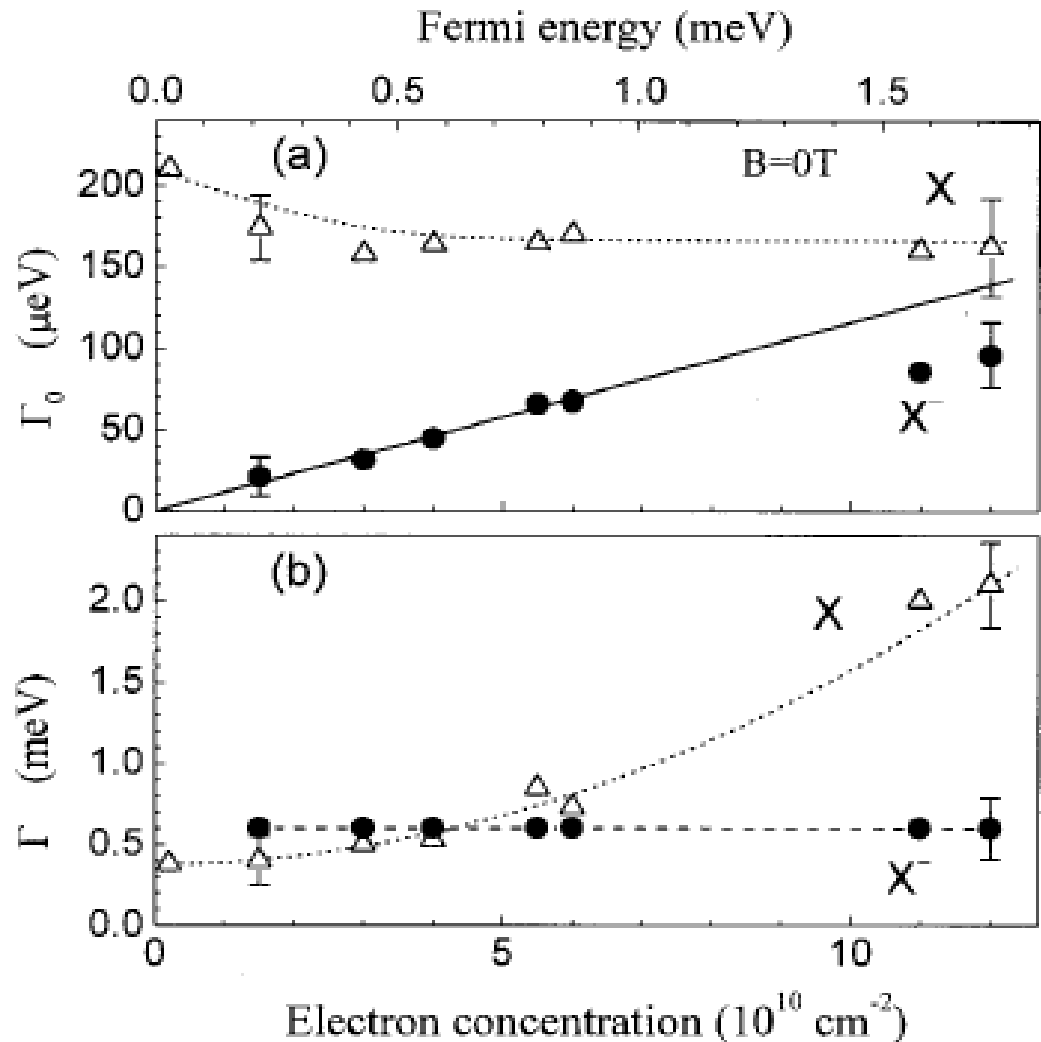
CdTe/CdMgTe 80A



ZnSe/ZnMgSSe 80A

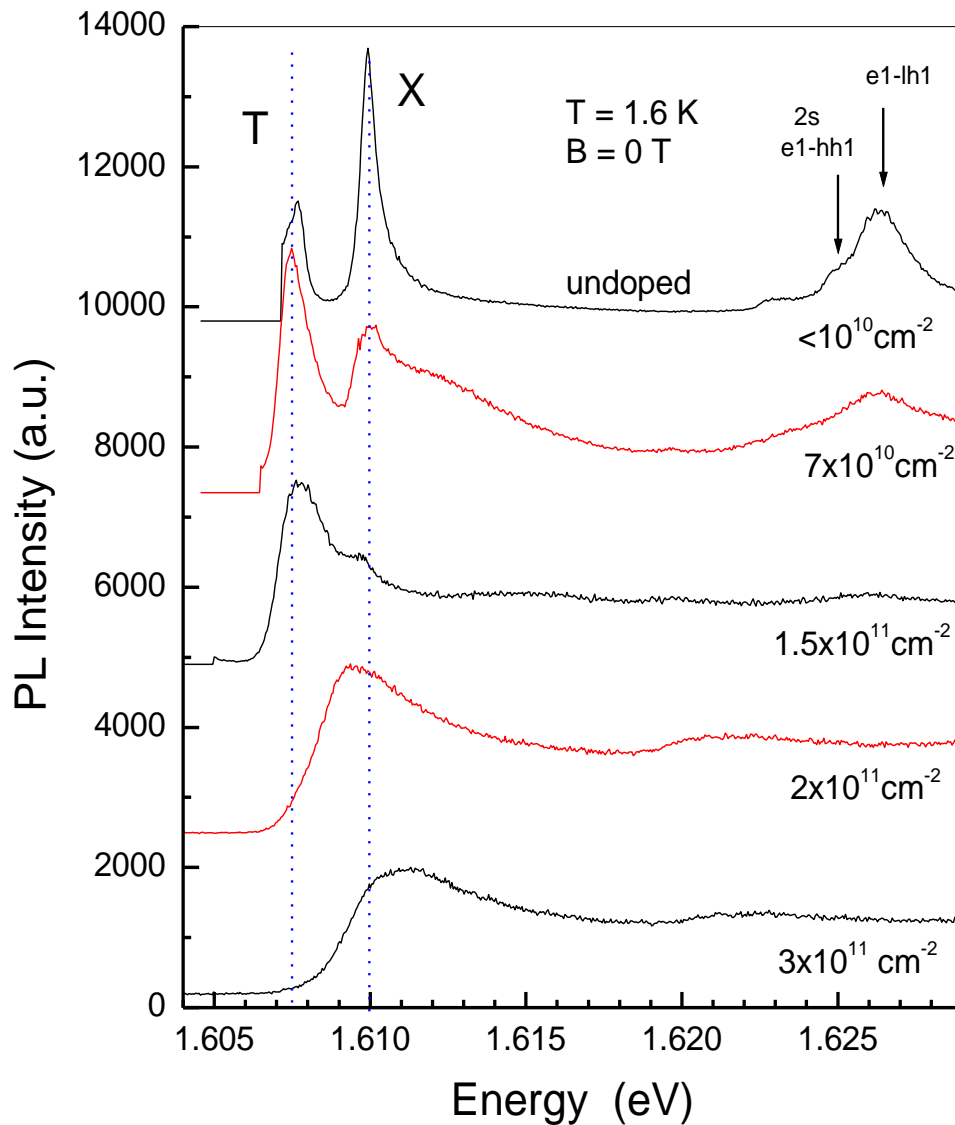


Сила осциллятора экситона не зависит от плотности 2DEG



Затухание экситона  
растет с ростом  
плотности

# Спектры поглощения (PLE) как функция концентрации



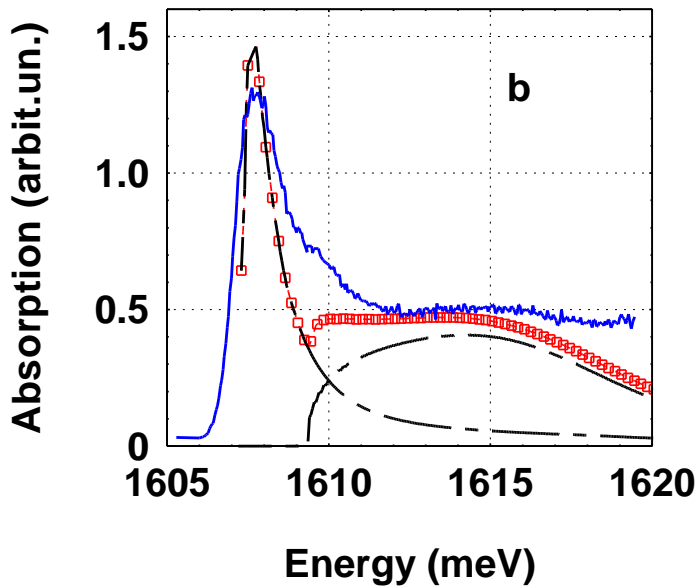
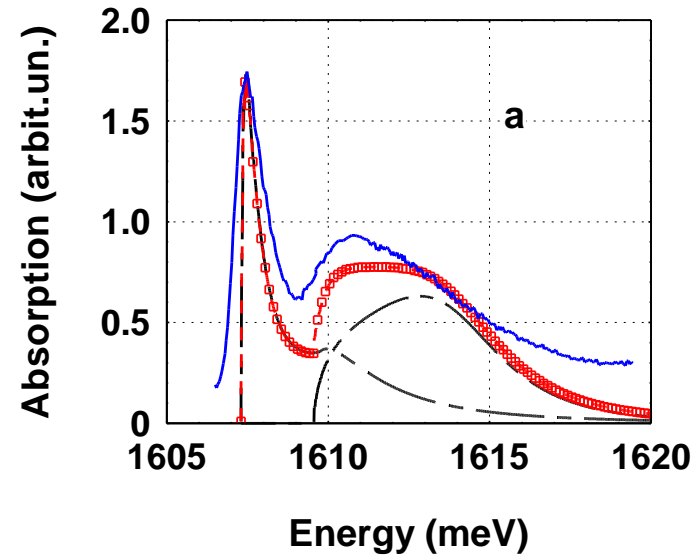


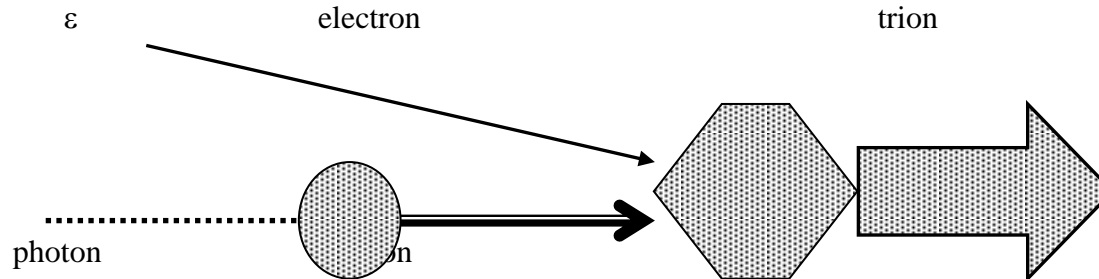
Figure 5: Absorption spectra of CdTe/CdMgTe quantum wells at different densities of free electrons. Solid lines are experimental spectra, symbols present results of calculation at  $E_F = 2.5$  meV (upper panel) and  $E_F = 10$  meV (lower panel), respectively. Dashed lines are contributions of trion and exciton.

Trion Zeeman splitting as a function  
of the electron density

The value of the exciton and trion Zeeman splitting?

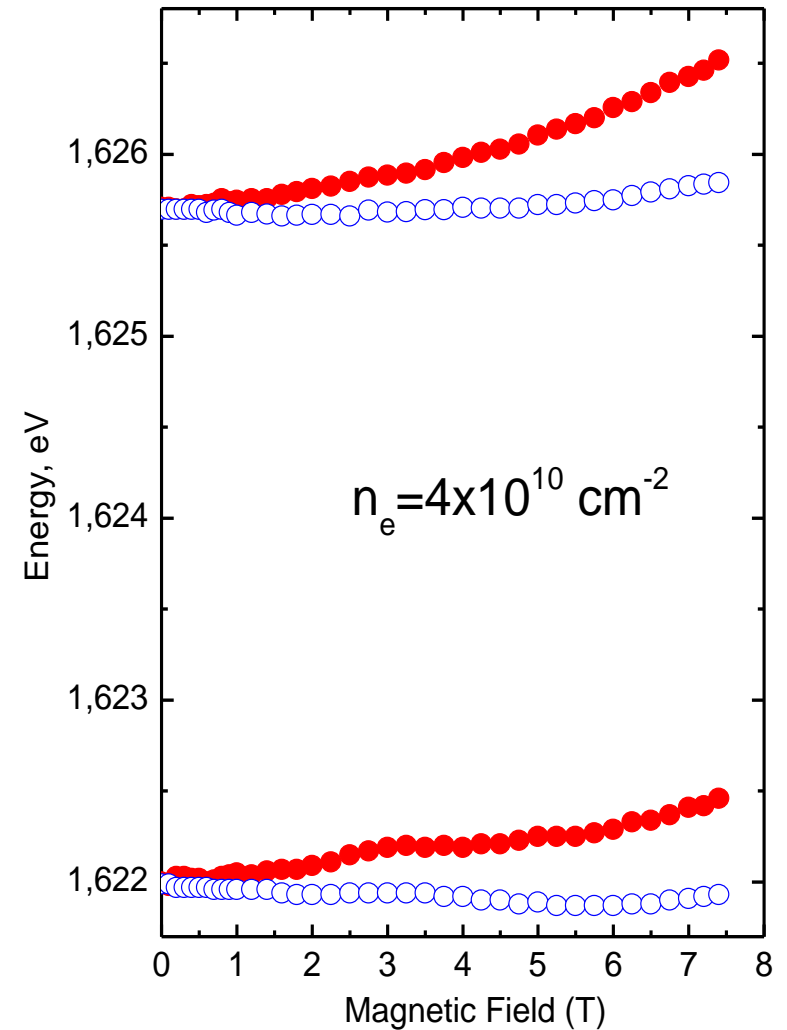
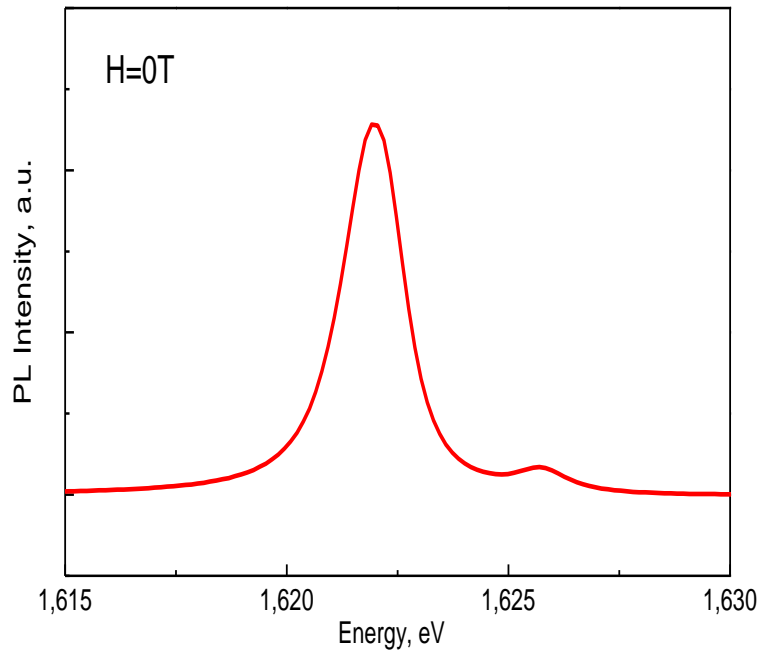
$$e_{init} + ph \rightarrow Tr = (Ex + e_{fin})$$

Because the initial and the final state of the electron are the same (the same spin and the same Landau level) we should see only the exciton Zeeman splitting on exciton and on trion line

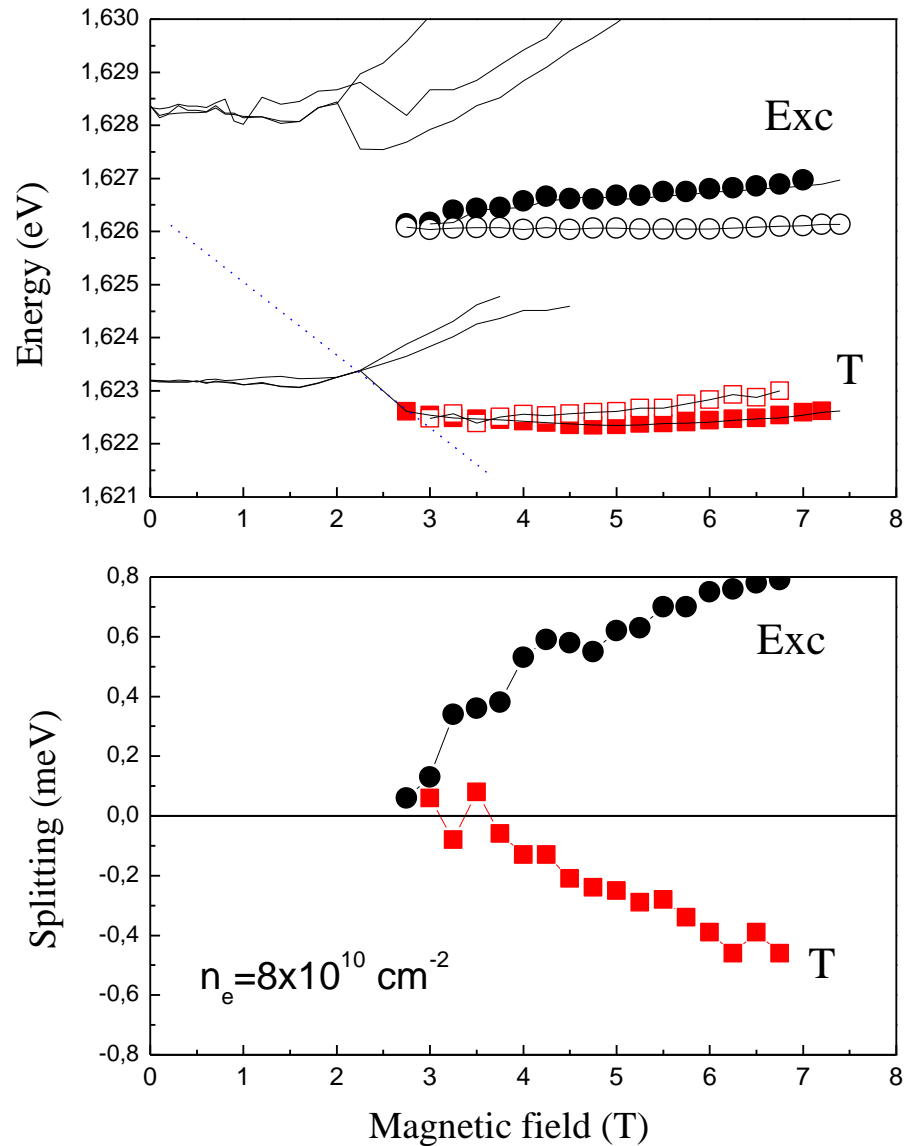


# Photoluminescence

In PL the exciton and trion Zeeman splitting are equal



# Exciton and trion Zeeman splitting at high electron concentrations





This is possible only in the case if the initial and final spin state of the electron are not the same –  
we need spin-flip

For spin-flip we need spin-orbital interaction.  
This can be the triplet-singlet splitting of the trion

In the initial state the photon creates virtual state of the triplet trion. Because of very fast spin-flip of one of the electrons in the final state we have the singlet trion (already real).  
This is the process reversal to the ExCR

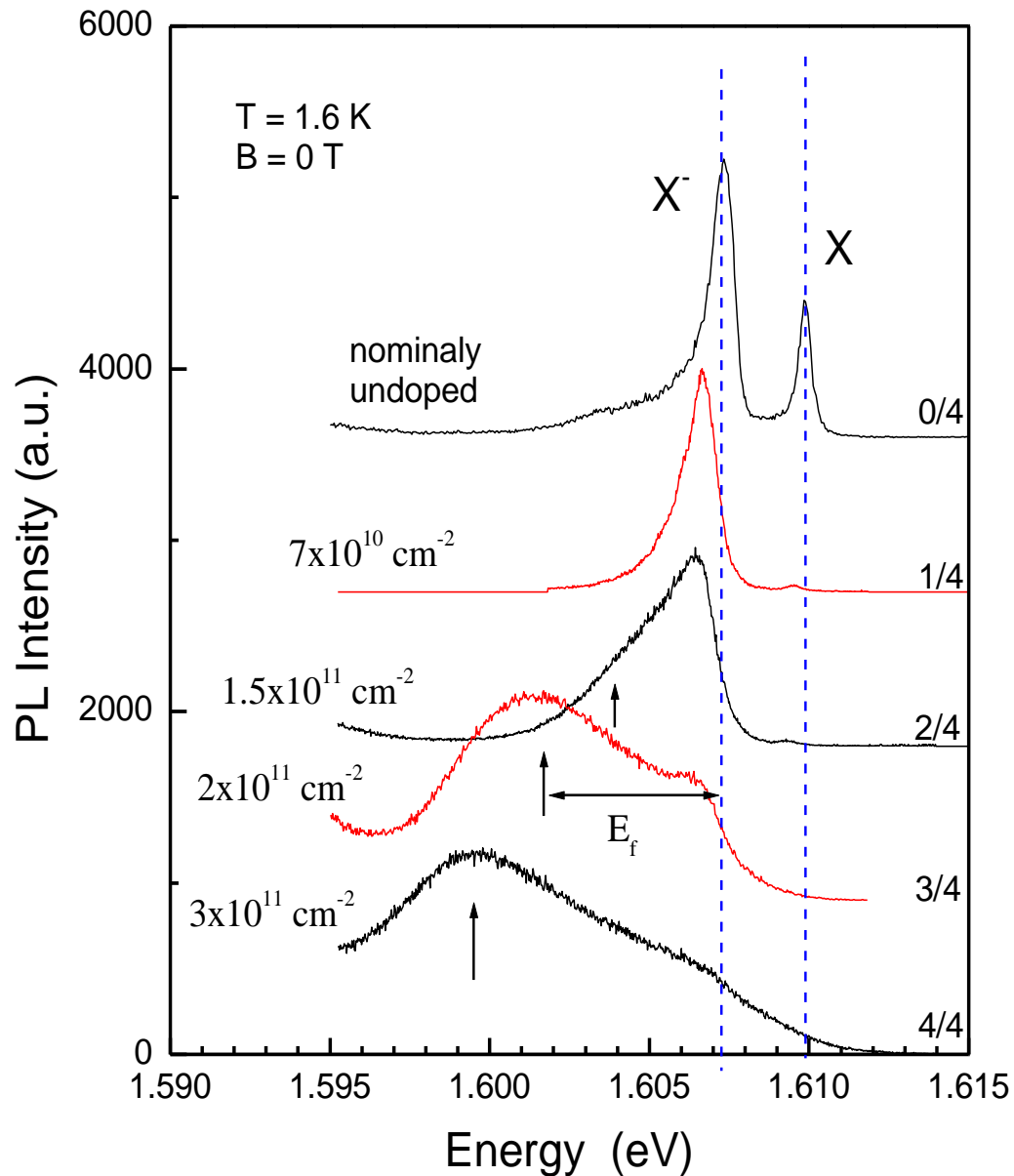
An incident photon creates a virtual trion in the triplet state. This trion produces a spin-flip with one of the electrons on the first Landau level. As a result, in the final state, we get a trion in the singlet state plus an electron on the second Landau level with opposite spin.

This reaction looks

$$e_1^{\uparrow} + e_2^{\uparrow} + ph \rightarrow Tr^t + e_1^{\uparrow} \rightarrow Tr^s + e_2^{\downarrow}$$

# Фотолюминесценция трионов

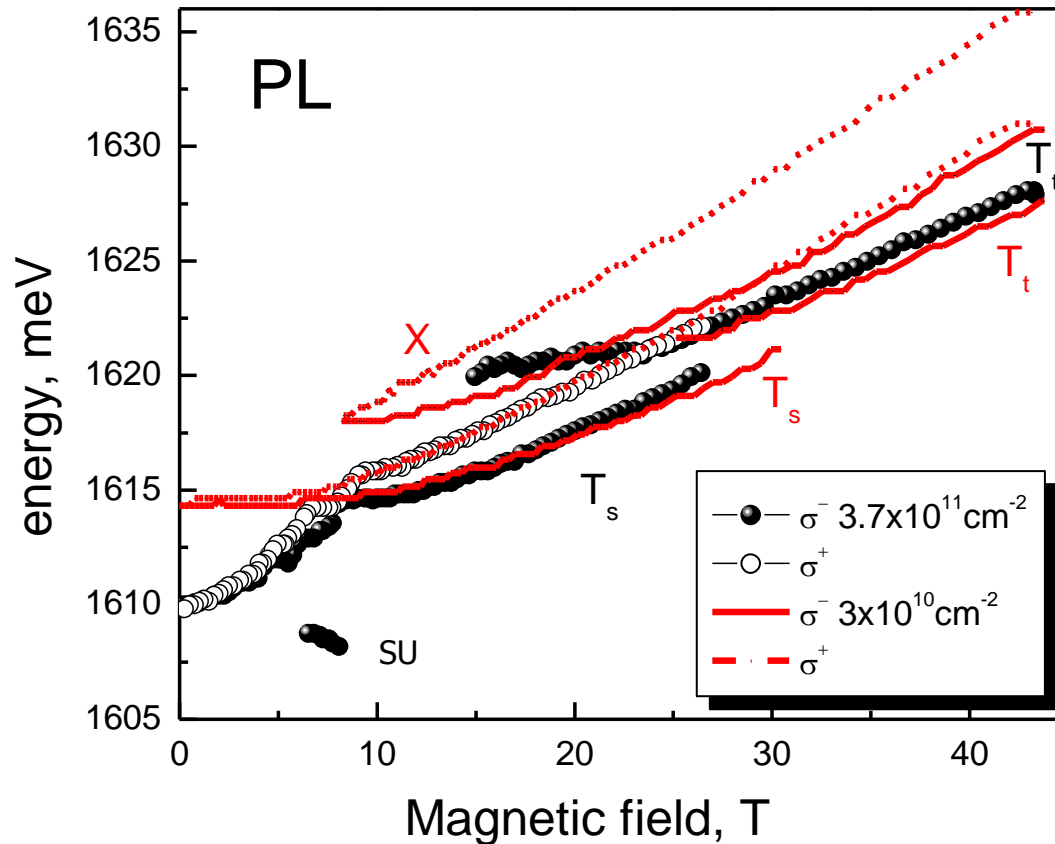
# Спектры ФЛ в зависимости от концентрации электронов



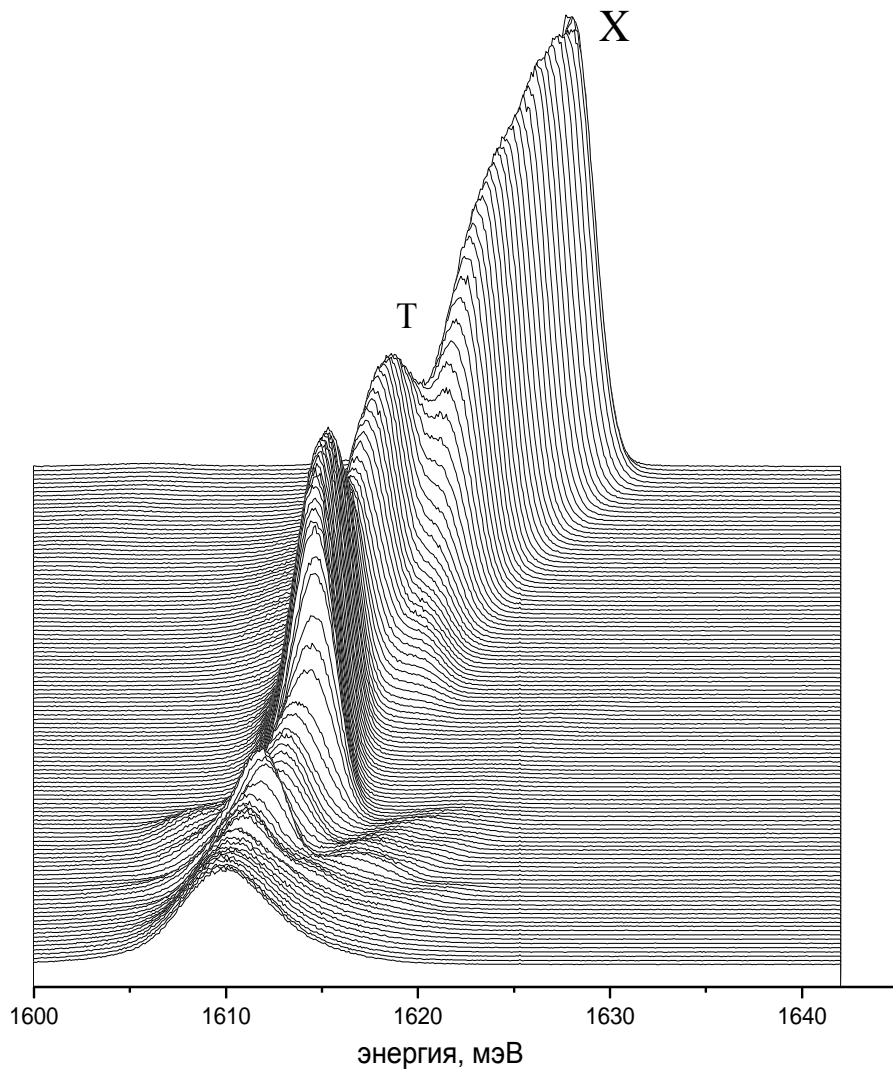
$$E_b^{\text{ex}} \gg E_F$$

$$E_b^{\text{tr}} \sim E_F$$

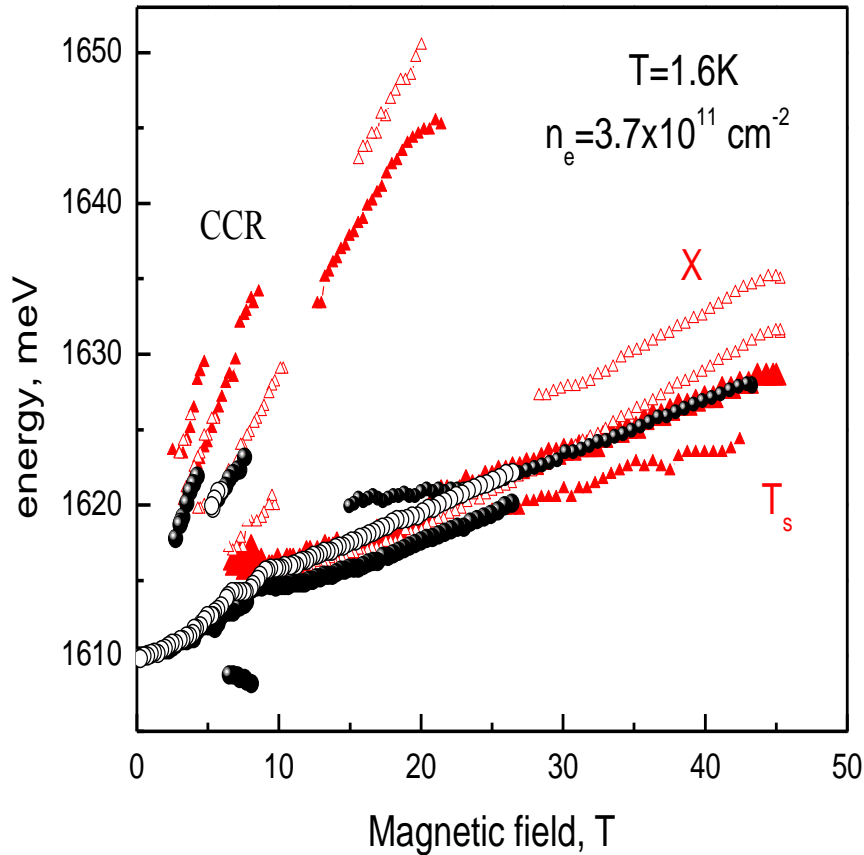
In heavily doped QW in zero magnetic fields the PL line is shifted to the low energies from its position in low doped structure. The value of this shift is of the order of Fermi energy



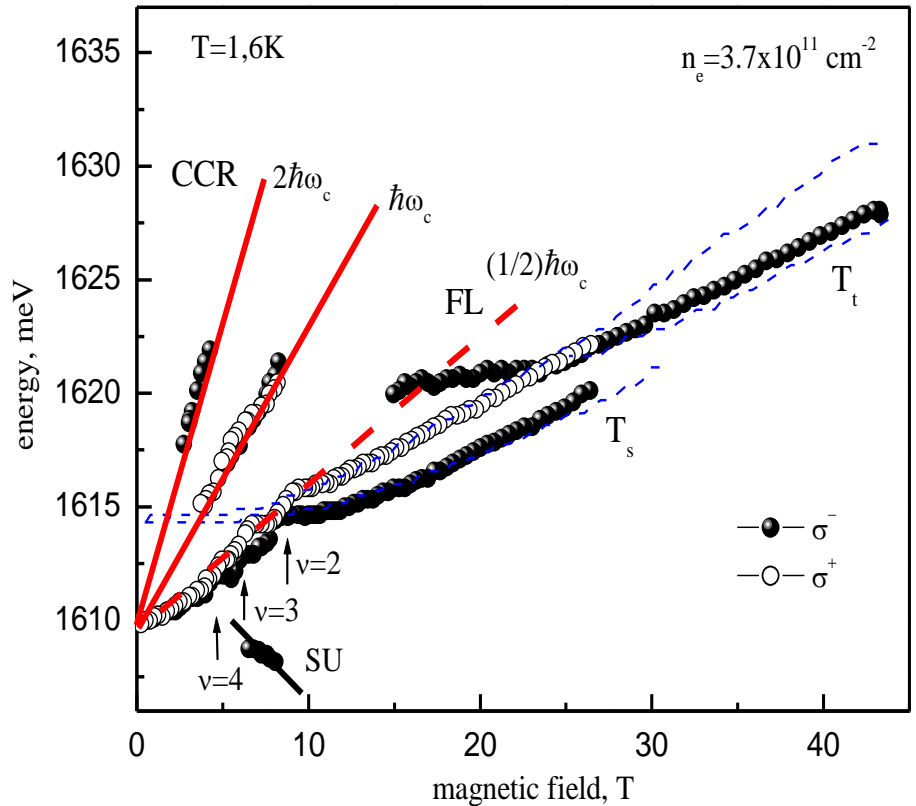
# В магнитном поле линии триона и экситона «возрождаются»



# Combined processes in PL



Comparison of PL and reflectivity



PL and SU

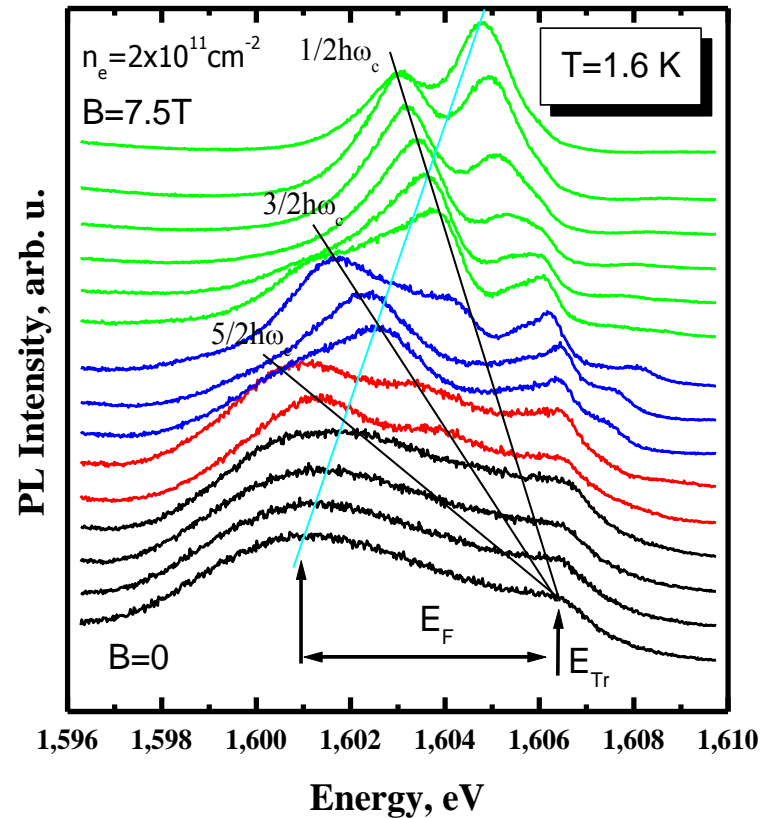
# Shake-up

## Shake up процессы SU

$$Tr \Rightarrow ph + e^*$$

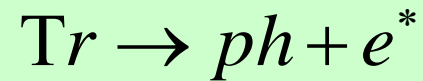
$$E_{tr} = \hbar\omega + (N + \frac{1}{2})\hbar\omega_e^c$$

$$\hbar\omega = E_{tr} - (N + \frac{1}{2})\hbar\omega_e^c$$





In Emission the initial state is: trion in a ground or excited states;



the final state is: an electron above Fermi level

The energy of the transition is  $\hbar\omega = E_{Tr} - E^* \leq E_{Tr} - E_F$

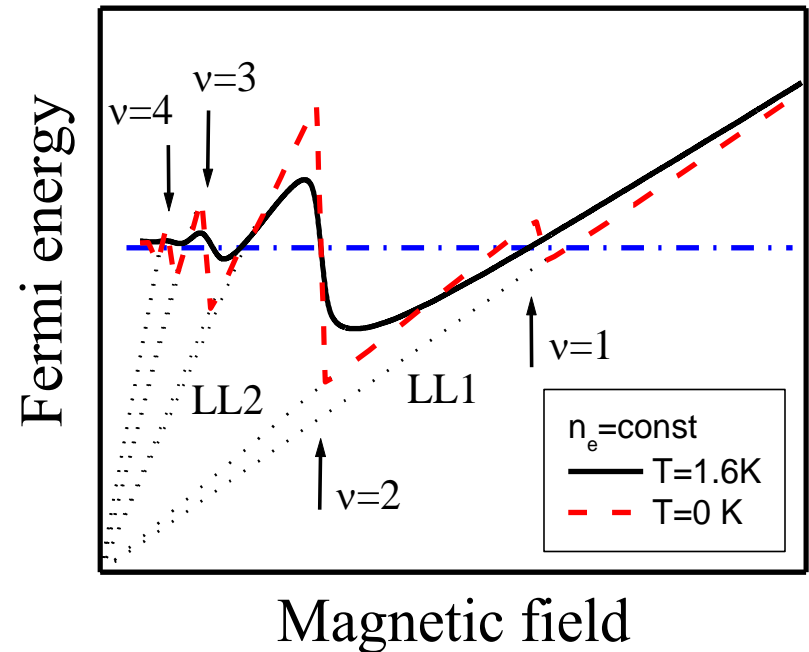
## Linear shift of the trion line in magnetic fields

In the final state after the trion recombination a free electron remains. It can appear in the unoccupied states above Fermi level

$$E_{tr} = \hbar\omega + E_F \Rightarrow \hbar\omega = E_{tr} - E_F$$

In magnetic fields the Fermi energy decreases as

$$\frac{1}{2} \hbar\omega_e^c$$



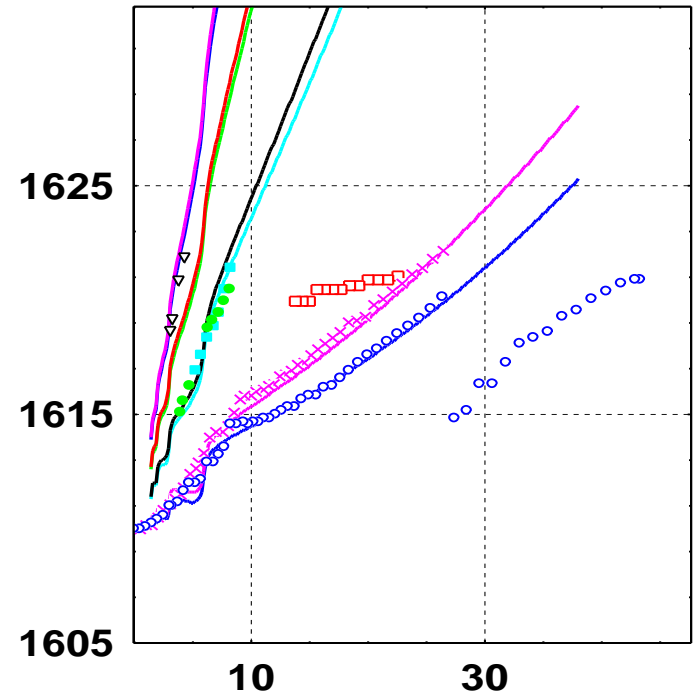
# Theory

$$\hbar\omega_{ph}^{\pm} = \hbar\Omega_c(n) - E_{tr} \pm \Delta(B) - E_F(B) + \alpha B + \beta B^2 + E_G$$

Figure gives the energy positions of maxima of emitted bands which are described by equation

The shape of the states is presented by the Gaussian form

$$\rho_n^{\pm}(E) = \frac{eB/(4\pi\hbar)}{\sqrt{2\pi\Gamma_n^2(B)}} \exp\left\{-\left[E - \hbar\omega_{ph}^{\pm}(n)\right]^2 / [2\Gamma_n^2(B)]\right\}$$



# Conclusions

In 2D structures containing electron gas the scattering effects are enhanced.

In the presence of magnetic fields the electron energy spectrum becomes discrete and the scattering processes reveal as combined exciton-electron processes.

In such processes we can see directly only the exciton transition but the state of the additional electron, which we can not see, reveals only in the final result.